## CSAP <br> Mathematics

1 Study the table below. The table shows the distance Ricky walks each dog after school.

## Distance Walked

| Name of Dog | Distance |
| :--- | :--- |
| Speedy (S) | 1 mile |
| Wags (W) | 1.75 miles |
| Cookie (C) | 0.25 miles |
| Jumper (J) | $1 \frac{1}{4}$ miles |
| Paws (P) | $\frac{1}{2}$ mile |

On the number line below, Point $S$ represents the distance Ricky walks Speedy. Label the points for the distances that Ricky walks each of the other dogs.


CSAP Mathematics Scoring Guide

## Item 1:

## Rubric

## Exemplary Response

- 



Score Points: Apply 2-point holistic rubric.
This item appeared at only one grade level.
Grade 5
Standard 1.1a: Number Sense
Subcontent Area: number and operations

Page 2
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## CSAP <br> Mathematics

2 Study the graph below. The graph shows the profit a clothing shop makes from selling sweaters and pairs of jeans.


Part A Complete the tables below by using the information from the graph to show the amount of profit for the number of items sold.

Clothing Shop Profits

| Number of <br> Sweaters Sold | Amount of Profit <br> (in dollars) |
| :---: | :---: |
| 10 |  |
| 15 |  |
| 25 |  |


| Number of <br> Pairs of Jeans Sold | Amount of Profit <br> (in dollars) |
| :---: | :---: |
| 10 |  |
| 15 |  |
| 25 |  |

Part B What is the amount of profit made from selling one sweater? In the space below, show your work and write your answer on the line.


Part C In one day, the shop sold 20 sweaters and 30 pairs of jeans. The sale of which of these items made more profit? In the space below, show your work to find the difference in profit and write your answers on the lines.
$\square$

CSAP Mathematics Scoring Guide

Item 2:
Rubric
Exemplary Response
Part A
Clothing Shop Profits

| Number of <br> Sweaters Sold | Amount of Profit <br> (in dollars) |
| :---: | :---: |
| 10 | 400 |
| 15 | 600 |
| 25 | 1,000 |


| Number of <br> Pairs of Jeans Sold | Amount of Profit <br> (in dollars) |
| :---: | :---: |
| 10 | 200 |
| 15 | 300 |
| 25 | 500 |

## Part B

- $\$ 40$

AND

- By dividing the profit made from selling 10 sweaters, $\$ 400$, by 10 , I can see that the profit made from selling 1 sweater is $\$ 40$.

OR

- Other valid process

CSAP Mathematics Scoring Guide

## Part C

- Sweaters made more profit

Difference in profit $\$ 200$
AND

- 20 sweaters $\times \$ 40$ per sweater $=\$ 800$

30 pairs of jeans $\times \$ 20$ per pair of jeans $=\$ 600$
$\$ 800-\$ 600=\$ 200$

OR

- Other valid process

Score Points: Apply 4-point holistic rubric.
This item appeared at two adjacent grade levels.

## Grade 5

Standard 3.4b: Data Analysis, Probability, and Statistics
Subcontent Area: data displays

## Grade 6

Standard 3.4a: Data Analysis, Probability, and Statistics
Subcontent Area: not classified

Page 6
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## CSAP <br> Mathematics

3 On the board in her classroom, Ms. Jones wrote the number sentence shown below.

$$
6 \times 18=?
$$

Study what three of her students said.


Part A In the space below, explain how Marni could know that the answer is more than 60 without solving the number sentence.

Part B In the space below, explain how Sally could use estimation to find that the answer is about 120 .
$\square$

Part C Nick wants to use his strategy to solve the problem shown below.

$$
7 \times 24=?
$$

In the space below, show how Nick would solve the problem using his strategy.

## Item 3:

## Rubric

## Exemplary Response

## Part A

- $6 \times 10$ equals 60 . Since 18 is greater than 10 , the answer must be greater than 60 .

OR

- Other valid response


## Part B

- Sally rounded 18 to 20 and then multiplied $6 \times 20$ to get 120 .


## OR

- Other valid response

Part C

- $(7 \times 20)+(7 \times 4)=168$

OR

- Other valid response

Score Points: Apply 3-point holistic rubric.
This item appeared at two adjacent grade levels.
Grade 5
Standard 1.6b: Number Sense
Subcontent Area: numbers and operations

## Grade 6

Standard 1.6a: Number Sense
Subcontent Area: numbers and operations

## CSAP

## Mathematics

4 Madeline is setting up dominoes in a line, as shown below. Each domino requires $\frac{7}{8}$ inch of space in the line.


Part A The line of dominoes will be 29 feet long. A box of dominoes contains 28 dominoes. Estimate the number of boxes Madeline will need. In the space below, show your work and write your estimate on the line.

Estimate $\qquad$ boxes

Part B After Madeline pushes over the first domino, each domino in the line will fall one after the other. It takes 0.8 seconds for 5 dominoes to fall. Estimate the time it will take for all the dominoes to fall. In the space below, show your work and write your estimate on the line.

## Estimate

$\qquad$ seconds

## Item 4:

## Rubric

## Exemplary Response

## Part A

- Estimate 12 boxes (accept range 12 to 15 boxes)


## AND

- Each domino requires $\frac{7}{8}$ inch $\approx 1$ inch,

29 feet $\approx 30$ feet and 12 inches per foot $\times 30$ feet $\approx 360$ inches,
so 360 inches $/ 1$ inch per domino $\approx 360$ dominoes, and
28 dominoes per box $\approx 30$ dominoes per box, so
360 dominoes $/ 30$ dominoes per box $\approx 12$ boxes.
OR

- Each domino requires $\frac{7}{8}$ inch $=0.875$ inch.

Approximately 360 inches/0.875 inch per domino $\approx 411$ dominoes, and
411 dominoes/ 28 dominoes per box $\approx 14.7$ boxes $\approx 15$ boxes.
OR

- Other valid response

CSAP Mathematics Scoring Guide

## Part B

- Estimate 72 seconds (accept range 54 to 80 )

AND

- 5 dominoes fall in 0.8 seconds $\approx 1$ second the time it takes 360 dominoes to fall is approximately 360 dominoes/5 dominoes per second $\approx 72$ seconds OR
- 29 feet $\times 12$ inches per foot $=348$ inches $\approx 350$ inches/ 1 inch per domino $\approx 350$ dominoes and 350 dominoes $\times 0.8$ seconds/ 5 dominoes $=0.8$ seconds $\times 70=56$ seconds OR
- Other valid response

Score Points: Apply 3-point holistic rubric.
This item appeared at only one grade level.

## Grade 7

Standard 6.3b: Operation and Calculation
Subcontent Area: number sense

## Page 12

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## CSAP

## Mathematics

5 Study the diagram below. The diagram shows a farmer's field. It takes the farmer approximately 6 minutes to plow a strip that measures 10 feet wide by 600 feet long.


Drawing not to scale

Part A What is the area, in square feet, that the farmer plows per minute? In the space below, show your work and write your answer on the line.

Part B At the same rate, approximately how long will it take the farmer to plow the entire field? In the space below, show your work and write your answer on the line.

## Approximately

$\qquad$ hours

Part C The next time he plows his field, the farmer uses new equipment. Now, the farmer can plow a strip that measures 600 feet long by 12 feet wide in approximately 6 minutes. Approximately how much time will the farmer save when plowing his entire field with his new equipment? In the space below, show your work and write your answer on the line.
$\square$

CSAP Mathematics Scoring Guide

## Item 5:

## Rubric

## Exemplary Response

## Part A

- 1,000 square feet per minute

AND

- One strip is $(600 \mathrm{ft})(10 \mathrm{ft})=6,000$ square feet. Since it takes 6 minutes to plow one strip, the area per minute is $\frac{6,000 \text { square feet }}{6 \text { minutes }}=1,000$ square feet per minute. OR
- Other valid response


## Part B

- Approximately 4 hours (or 240 minutes)


## AND

- Area of entire field $=(500 \mathrm{ft})(300 \mathrm{ft})+(300 \mathrm{ft})(300 \mathrm{ft})=150,000+90,000=$ 240,000 square feet. At the same rate, it will take $\frac{240,000 \text { square feet }}{1,000 \text { square feet/minute }}=$ 240 minutes, or $240 \div 60=4$ hours.


## OR

- Other valid response

CSAP Mathematics Scoring Guide

## Part C

- Approximate time saved 40 minutes


## AND

- With the new equipment, each strip will have an area of $(600 \mathrm{ft})(12 \mathrm{ft})=7,200$ square feet, so the new rate will be $\frac{7,200 \text { square feet }}{6 \text { minutes }}=1,200$ square feet per minute.
At that rate, the entire field will take $\frac{240,000 \text { square feet }}{1,200 \text { square feet } / \text { minute }}=200$ minutes.
So the new equipment will save $240-200=40$ minutes.
OR
- Other valid response

Score Points: Apply 4-point holistic rubric.
This item appeared at only one grade level.

## Grade 8

Standard 6.4a: Patterns, Functions, and Algebra
Subcontent Area: proportional thinking

## CSAP

## Mathematics

 From your punch-out tools, use the protractor to help you solve this problem.Part A The circle graph below shows the proportions of a publisher's books sold to schools, bookstores, and libraries. Label the circle graph by writing the percents on the lines.


Part B The publisher sold 350,000 books last year. How many books were sold to bookstores? In the space below, show your work and write your answer on the line.


> publisher-company that prepares books

CSAP Mathematics Scoring Guide

## Item 6:

Rubric

## Exemplary Response

## Part A



- Accept range: Libraries $14 \%$ to $15 \%$, Bookstores $20 \%$ to $21 \%$, Schools $64 \%$ to $65 \%$


## Part B

- 70,000 books

AND

- $350,000 \operatorname{books}(20 \%)=350,000(0.20)=70,000$ books

OR

- Other valid response

Score Points: Apply 2-point holistic rubric.
This item appeared at only one grade level.

## Grade 8

Standard 3.1a: Data Analysis, Probability, and Statistics
Subcontent Area: proportional thinking

Page 18
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## CSAP

## Mathematics

7 Russell hits a golf ball, the path of which can be approximated by the equation shown below.

$$
y=-\frac{1}{400}(x-140)^{2}+49
$$

$y=$ height of the ball, in yards
$x=$ horizontal distance, in yards

Part A Find the height of the ball after it has traveled a horizontal distance of 100 yards. In the space below, show your work and write your answer on the line.
$\square$

Part B What do the $x$-intercepts represent in the context of the problem? On the lines below, explain your reasoning.

Part C Study the diagram below. The diagram shows a tree at a horizontal distance of 160 yards from the starting point of the ball. The tree is 139 feet tall.


By how many feet will the ball clear the tree? In the space below, show your work and write your answer on the line.


CSAP Mathematics Scoring Guide

## Item 7:

## Rubric

## Exemplary Response

Part A

- Height 45 yards

AND

- $h=-\frac{1}{400}(100-140)^{2}+49$
$h=-\frac{1}{400}(-40)^{2}+49$
$h=-\frac{1}{400}(1,600)+49$
$h=-4+49$
$h=45$
OR
- Other valid process


## Part B

- The $x$-intercepts represent the points at which the ball is at a height of zero yards, which are at the beginning of the hit and after the ball lands.

OR

- Other valid process

CSAP Mathematics Scoring Guide

## Part C

- 5 feet

AND

- $h=-\frac{1}{400}(160-140)^{2}+49$
$h=-\frac{1}{400}(400)+49$
$h=-1+49$

48 yards $\times 3$ feet per yard $=144$ feet
OR

- Other valid process

Score Points: Apply 3-point holistic rubric.
This item appeared at two adjacent grade levels.

## Grade 9

Standard 2.3a: Patterns, Functions, and Algebra
Subcontent Area: not classified
Grade 10
Standard 2.3a: Patterns, Functions, and Algebra
Subcontent Area: not classified

## CSAP <br> Mathematics

8 The snow sports club in Montrose surveyed its members. The results of the survey are shown below.
$35 \%$ of the members downhill ski only.
$20 \%$ of the members cross-country ski only.
$45 \%$ of the members snowboard only.
What is the fewest number of people that could be members of the club? In the space below, show your work and write your answer on the line.
$\square$

CSAP Mathematics Scoring Guide

## Item 8:

Rubric
Exemplary Response

- 20 people

AND

- If 100 people were in the club, the ratio of each type would be 35:20:45. These numbers are all divisible by 5 , giving 7:4:9, which is fully reduced. Summing gives 20 members.


## OR

- Other valid response

Score Points: Apply 2-point holistic rubric.
This item appeared at two adjacent grade levels.
Grade 9
Standard 6.1a: Operation and Calculation
Subcontent Area: not classified
Grade 10
Standard 6.1a: Operation and Calculation
Subcontent Area: not classified

## CSAP

## Mathematics

9 Karen will enlarge the photograph shown below.


Drawing not to scale

Part A While maintaining the ratio of height to width, Karen will increase the height to 12.5 inches. What will be the width of the enlarged photograph? In the space below, show your work and write your answer on the line.


Part B Karen will use a copy machine to enlarge the photograph. The copy machine increases the area of the photograph by any percentage, while maintaining the height-towidth ratio of the original. By what percent does Karen need to enlarge the area of the original photograph? In the space below, show your work and write your answer on the line.
$\square$

Part C Before framing, Karen surrounded the enlarged photograph with a 2-inch border. On the lines below, explain the effect of the border on the proportional relationship between the height and width.

## Item 9:

## Rubric

## Exemplary Response

## Part A

- 7.5 inches

AND

- $12.5 \times 3 \div 5=7.5$ inches


## OR

- Other valid process


## Part B

- 625 percent

AND

- $(12.5 \times 7.5) \div(5 \times 3) \times 100=625 \%$


## OR

- Other valid process


## Part C

- The framed photograph does not have the same ratio because the ratios of the original and enlarged photographs are 5 to 3, while the ratio of the framed photograph is $16 \frac{1}{2}$ to $11 \frac{1}{2}$.
This is not an equivalent ratio because it does not reduce to $5 / 3$.
OR
- Other valid reponse comparing $5: 3$ to $16.5: 11.5$

NOTE: A student may draw diagrams in the space available at the bottom of the page.
Diagrams may be referred to in the student's explanation.
Score Points: Apply 3-point holistic rubric.
This item appeared at only one grade level.

## Grade 10

Standard 6.1a: Operation and Calculation
Subcontent Area: not classified

