CMAS Grade 4 Mathematics Performance Level Descriptors (Based on PARCC)

In 2018, Colorado will continue to use the performance level descriptors (PLDs) that were developed in collaboration with the Partnership for Assessment of Readiness for College and Careers (PARCC) consortium to describe performance on the CMAS assessments.

	Grade 4 Math : Sub-Claim A The student solves problems involving the Major Content for the grade/course with connections to the Standards for Mathematical Practice.			
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Fractions and	Compares decimals to hundredths;	Given a visual model and/or	Given a visual model and/or	Given a visual model and/or
Decimals	uses decimal notations for fractions	manipulatives, compares decimals	manipulatives, compares decimals	manipulatives, compares decimals
4.NF.1-2	with denominators 10 or 100.	to hundredths:	to hundredths; uses decimal	to hundredths; uses decimal
4.NF.2-1	Compares fractions, with like or	Expresses a fraction with	notations for fractions (tenths and	notations for fractions (tenths and
4.NF.A.Int.1	unlike numerators and	denominator 10 as an equivalent	hundredths); compares fractions,	hundredths); compares fractions
4.NF.5	denominators, by creating	fraction with denominator 100.	with like or unlike numerators and	with like denominators.
4.NF.6	equivalent fractions with common	Uses decimal notation for	denominators by comparing to a	
4.NF.7	denominators, comparing to a	fractions with denominators 10 or	benchmark fraction.	
4.NF.Int.1	benchmark fraction and generating	100.		
4.NF.Int.2	equivalent fractions.	Compares fractions, with like or	Recognizes that decimals and	
		unlike numerators and	fractions must refer to the same	
	Recognizes that decimals and	denominators, by creating	whole in order to compare.	
	fractions must refer to the same	equivalent fractions with common		
	whole in order to compare.	denominators and comparing to a	Shows results using symbols.	
		benchmark fraction.		
	Shows results using symbols.		Solves simple word problems	
		Recognizes that decimals and	requiring fraction comparison with	
	Demonstrates the use of	fractions must refer to the same	scaffolding.	
		whole in order to compare.		
	fractional equivalence and			
	ordering when solving simple word	Shows results using symbols.		
	problems requiring fraction			
	comparison.	Solves simple word problems		
		requiring fraction comparison.		
	Converts a simple fraction to a			
	denominator of 10 or 100 and			
	writes as a decimal (e.g.,1/2 =			

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	5/10 = .5, ¼ = 25/100 = 0.25, 1/20 = 5/100 = 0.05). Adds fractions with denominators of 10 and 100.				
Fractions 4.NF.3a 4.NF.3b-1 4.NF.3c 4.NF.3d 4.NF.Int.1	mathematical and real-world problems involving the addition and subtraction of fractions and mixed numbers with like denominators by joining and separating parts referring to the same whole, and justifying the solution by using a visual model. Decomposes a fraction into a sum of fractions with the same denominator in more than one way and records the decomposition	and word problems involving the addition and subtraction of fractions and mixed numbers with like denominators by joining and separating parts referring to the same whole. Decomposes a fraction into a sum of fractions with the same denominator in more than one way	manipulatives, solves mathematical problems involving the addition and subtraction of fractions with like denominators by joining and separating parts referring to the same whole. Decomposes a fraction into a sum of fractions with the same denominator in more than one	Using visual models and/or manipulatives, solves mathematical problems involving the addition and subtraction of fractions with like denominators by joining and separating parts referring to the same whole.	
		Using visual models and/or	Using visual models and/or	Using visual models and/or	
		6	0	manipulatives, solves mathematical	
4.NF.4a 4.NF.4b-1 4.NF.4b-2	world problems by recognizing that fraction <i>a/b</i> is a multiple of 1/ <i>b</i> and uses that construct to multiply a fraction by a whole number.	and real- world problems by	problems by recognizing that fraction <i>a/b</i> is a multiple of 1/b and uses that construct to multiply a	problems by recognizing that	
-			Interprets multiplication equations		
4.0A.1-1 4.0A. 1-2	statements of multiplicative comparisons as multiplicative	as comparisons or represents statements of multiplicative comparisons as multiplicative equations.	statements of multiplicative comparisons as multiplicative	as comparisons or represents statements of multiplicative comparisons as multiplicative equations.	

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	Distinguishes multiplicative comparisons. Uses multiplication or division to solve multi-step word problems involving multiplicative comparisons.	Uses multiplication or division to solve one- or two-step word	Uses multiplication or division to solve scaffolded word problems involving multiplicative comparisons.	
	Uses a symbol for the unknown number.			
Multi-step Problems 4.OA.3-1 4.OA.3-2 4.NBT.5-1 4.NBT.5-2 4.NBT.6-1 4.NBT.6-2 4.Int.2 4.Int.3 4.Int.4 4.Int.5	three-or four-digit by a one-digit number or two two-digit numbers. Finds whole number quotients and remainders with up to four -digit dividends and one-digit divisors and interprets remainders as appropriate. Chooses from a variety of	problems using the four operations with whole numbers: in multiplying a three-digit by a one-digit number or two two-digit numbers Finds whole number quotients and remainders with up to three-digit dividends and one-digit divisors and interprets remainders as appropriate. Chooses from a variety of strategies to solve these problems.	problems using the four operations with whole numbers: in multiplying a three-digit by a one-digit number or two two-digit numbers. Finds whole number quotients and remainders with up to three-digit dividends and one-digit divisors. Chooses from a variety of strategies to solve these problems. Can only solve two-step problems	or two two-digit numbers. Finds whole number quotients and remainders with up to three-digit dividends and one-digit divisors.
Place Value 4.NBT.1 4.NBT.2 4.NBT.3 4.NBT.Int.1	recognizes a digit in one place represents 10 times as much as it represents in the place to its right.	In any four-digit whole number, recognizes a digit in one place represents 10 times as much as it represents in the place to its right.	In any three-digit whole number, recognizes a digit in one place represents 10 times as much as it represents in the place to its right.	In any three-digit whole number, recognizes a digit in one place represents 10 times as much as it represents in the place to its right.
	Reads, writes and compares multi- digit whole numbers using base-10	Reads, writes and compares four- digit whole numbers using base-10	Reads, writes and compares three- digit whole numbers using base-10	

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	expanded form and inequality symbols (>, <, =), rounds to any	numerals, number names in expanded form and inequality symbols (>, <, =), and rounds to any place.	numerals, number names in expanded form and inequality symbols (>, <, =), and rounds to any place with scaffolding.	
Addition and Subtraction 4.NBT.4-1 4.NBT.4-2 4.Int.7 4.Int.8	Solves multiple -step word and other problems by adding or subtracting multi-digit whole numbers using the standard	Solves two -step word problems and other problems by adding and subtracting multi-digit whole numbers using the standard algorithm.	numbers using the standard	Solves one-step word problems and other problems by adding and subtracting multi-digit whole numbers using the standard algorithm with limited accuracy.

	Grade 4 Math: Sub-Claim B The student solves problems involving the Additional and Supporting Content for the grade/course with connections to the Standards			
		for Mathema	•	
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Operations	Recognizes that a whole number is	Recognizes that a whole number is	Recognizes that a whole number is	Recognizes that a whole number is
and Factors	a multiple of each of its factors,	a multiple of each of its factors,	a multiple of each of its factors,	a multiple of each of its factors,
4.OA.4-1	and within the range of 1-100, finds	and within the range of 1-100	and within the range of 1-100 finds	and within the range of 1-100
4.OA.4-2	all factor pairs and determines	finds factor pairs or determines	factor pairs or determines	identifies factor pairs or multiples
4.OA.4-3	multiples of whole numbers.	multiples of whole numbers.	multiples of whole numbers.	of whole numbers.
4.OA.4-4				
	Determines whether a whole	Determines whether a whole	Determines, with scaffolding,	
	number in the range 1-100 is prime	number in the range 1-100 is	whether a whole number in the	
	or composite.	prime or composite.	range 1-100 is prime or composite.	
Measurement	Solves measurement word	Solves measurement word	Solves mathematical measurement	Solves mathematical measurement
and	problems involving whole numbers	problems involving whole	problems involving whole numbers	problems involving whole numbers

	Grade 4 Math: Sub-Claim B The student solves problems involving the Additional and Supporting Content for the grade/course with connections to the Standards for Mathematical Practice.			
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Conversion 4.MD.1 4.MD.2-1 4.MD.2-2 4.MD.3 4.Int.6	and perimeter – including those in which side lengths are missing – using all four operations. Solves measurement word problems which include calculation of area and perimeter – including those in which side lengths are missing – using addition, subtraction, and multiplication of simple fractions. Records measurement equivalents in a two-column table. Uses knowledge of measurement units within one system to solve word problems, real-world problems, and mathematical problems involving converting from larger units to smaller units.	Level 4: Met Expectations numbers which include calculation of area and perimeter – when information about side lengths is provided – using all four operations. Solves measurement word problems which include calculation of area and perimeter – when information about side lengths is provided – using addition, subtraction, and multiplication of simple fractions. Records measurement equivalents in a two-column table. Uses knowledge of measurement units within one system to solve word problems, real-world	Level 3: Approached Expectations using all four operations. Solves mathematical measurement problems using addition, subtraction, and multiplication of simple fractions.	using all four operations. Solves mathematical measurement problems using addition and subtraction of simple fractions.
	quantities using diagrams such as number line diagrams that require students to provide the	Represents measurement quantities using diagrams such as number line diagrams that feature a measurement scale.		
Represent and Interpret Data	Makes a line plot to display a data set of measurements in fractions of		set of measurements in fractions of	Identifies a correct line plot that displays a data set of measurements in fractions of a unit

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4.MD.4-2	solve problems involving information in the line plots and evaluates the solution in relation to the data.	problems involving information in the line plot.	or 4.	with like denominators of 2 or 4.
Measurement 4.MD.5 4.MD.6 4.MD.7	and that angle measures are additive. Understands and applies concepts of angle measurement recognizing	Understands and applies concepts of angle measurement.	Understands and applies concepts of angle measurement.	Understands and identifies concepts of angle measurement.
	that angles are measured in reference to a circle. Uses a protractor to measure and sketch angles.		Uses a protractor to measure angles.	
	Solves mathematical and real-	world problems by composing and decomposing angles.		
	Solves mathematical and real- world angle problems, including problems that require the use of equations with a symbol for the unknown angle measure.			
Lines, Angles and Shapes 4.G 1 4.G.2	Draws and identifies points, lines, line segments, rays, angles (right, obtuse and acute), perpendicular lines, parallel lines, lines of symmetry and right	angles (right, obtuse and acute),	Identifies points, lines, line segments, rays, angles (right, obtuse and acute), perpendicular lines, parallel lines, lines of symmetry and right triangles, and	Identifies points, lines, line segments, rays, angles (right, obtuse and acute), perpendicular lines, parallel lines, lines of symmetry and right triangles.

	Grade 4 Math: Sub-Claim B The student solves problems involving the Additional and Supporting Content for the grade/course with connections to the Standards for Mathematical Practice.				
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations	
	triangles, and use any of these to classify or describe two- dimensional figures.	triangles, and use some of these to classify two-dimensional figures.	use some of these to classify quadrilaterals and triangles.		
Analyze Patterns 4.OA.5		pattern that follows a given rule and identifies explicit features of	Generates a number or shape pattern that follows a given rule.	ldentifies a number or shape pattern that follows a given rule.	

		Grade 4 Mat	th: Sub-Claim C	
			l appropriate mathematical reasoning	
	critiquing the r	easoning of others and/or attending	to precision when making mathema	tical statements.
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Properties of	In connection with the content			
Operations	knowledge, skills, and abilities			
4.C.1-1	described in Sub-claims A and B,	described in Sub-claims A and B, the	described in Sub-claims A and B, the	described in Sub-claims A and B, the
4.C.1-2	the student clearly constructs and	student clearly constructs and	student constructs and	student constructs and
4.C.2	communicates a complete written	communicates a complete written	communicates a written response	communicates an incomplete
4.C.3	response based on	response based on	based on explanations/reasoning	written response based on
	explanations/reasoning using the:	explanations/reasoning using the:	using the:	explanations/reasoning using the:
	 properties of operations 			
	 relationship between addition 			
	and subtraction	and subtraction	and subtraction	and subtraction
	 relationship between 			
	multiplication and division	multiplication and division	multiplication and division	multiplication and division
	 identification of arithmetic 			
	patterns	patterns	patterns	patterns
	Response may include:	Response may include:	Response may include:	Response may include:
	 a logical/defensible approach 	 a logical/defensible approach 	 a logical approach based on a 	 an approach based on a
	based on a conjecture and/or	based on a conjecture and/or	conjecture and/or stated	conjecture and/or stated or
	stated assumptions, utilizing	stated assumptions, utilizing	assumptions	faulty assumptions

	Grade 4 Math: Sub-Claim C				
		student expresses grade/course-level			
			asoning of others and/or attending to precision when making mathematical statements.		
	Level 5: Exceeded Expectations	Level 4: Met Expectations		Level 2: Partially Met Expectations	
	 mathematical connections (when appropriate) an efficient and logical progression of steps with appropriate justification precision of calculation correct use of grade-level vocabulary, symbols and labels justification of a conclusion evaluation of whether an argument or conclusion is generalizable evaluating, interpreting and critiquing the validity of other's responses, reasonings, and approaches, utilizing mathematical connections (when appropriate). Provides a counter-example where applicable. 	 mathematical connections (when appropriate) a logical progression of steps precision of calculation correct use of grade-level vocabulary, symbols and labels justification of a conclusion evaluation of whether an argument or conclusion is generalizable evaluating, interpreting and critiquing the validity of other's responses, reasonings, and approaches, utilizing mathematical connections (when appropriate). 	 a logical, but incomplete, progression of steps minor calculation errors some use of grade-level vocabulary, symbols and labels partial justification of a conclusion based on own calculations evaluating the validity of other's responses, approaches and conclusions. 		
Concrete			In connection with the content	In connection with the content	
Referents and	U		knowledge, skills, and abilities	knowledge, skills, and abilities	
Diagrams				described in Sub-claims A and B, the	
4.C.4-1	the student clearly constructs and	•	student constructs and	student constructs and	
4.C.4-2 4.C.4-3	<u> </u>	communicates a well- organized and	-	communicates an incomplete	
4.C.4-3 4.C.4-4				response based on operations using	
4.C.4-4 4.C.4-5		operations using concrete referents		concrete referents such as diagrams	
4.C.4-5 4.C.7-1	_	such as diagramsincluding number		 including number lines (provided 	
4.C.7-1 4.C.7-2			(provided in the prompt) –	in the prompt) – connecting the	
4.C.7-2 4.C.7-3			connecting the diagrams to a	diagrams to a written (symbolic)	
4.C.7-3 4.C.7-4		diagrams to a written (symbolic)	written (symbolic) method, which may include: • a logical approach based on a	 method, which may include: a conjecture and/or stated or faulty assumptions 	

	Grade 4 Math: Sub-Claim C			
		tudent expresses grade/course-level		
	critiquing the reasoning of others and/or attending to precision when making mathematical statements.			
	Level 5: Exceeded Expectations	Level 4: Met Expectations		Level 2: Partially Met Expectations
	 may include: a logical approach based on a conjecture and/or stated assumptions, utilizing mathematical connections (when appropriate) an efficient and logical progression of steps with appropriate justification precision of calculation correct use of grade-level vocabulary, symbols and labels justification of a conclusion evaluation of whether an argument or conclusion is generalizable evaluating, interpreting, and critiquing the validity of other's responses, approaches, and reasoning, and providing a counter-example where applicable. 		 conjecture and/or stated assumptions a logical, but incomplete, progression of steps minor calculation errors some use of grade-level vocabulary, symbols and labels partial justification of a conclusion based on own calculations. evaluating the validity of other's responses, approaches and conclusions 	 accepting the validity of other's responses.
		-	knowledge, skills, and abilities	In connection with the content knowledge, skills, and abilities
				described in Sub-claims A and B, the
-	the student clearly constructs and	-		student constructs and
	-	communicates a well-organized and complete response by:	communicates a complete response by:	communicates an incomplete response by:
Flawed	 presenting and defending 	 presenting and defending 	 presenting solutions to multi- 	 presenting solutions to
4.C.5-1	solutions to multi-step	solutions to multi-step problems	• presenting solutions to multi- step problems in the form of	scaffolded two-step problems in
4.C.5-2	problems in the form of valid	in the form of valid chains of	valid chains of reasoning, using	the form of valid chains of

	Grade 4 Math: Sub-Claim C In connection with content, the student expresses grade/course-level appropriate mathematical reasoning by constructing viable arguments, critiquing the reasoning of others and/or attending to precision when making mathematical statements.			
	Level 5: Exceeded Expectations	Level 4: Met Expectations	-	Level 2: Partially Met Expectations
4.C.5-3 4.C.5-4 4.C.5-5 4.C.5-6 4.C.6-1 4.C.6-2 4.C.6-3	 chains of reasoning, using symbols such as equal signs appropriately evaluating explanation/reasoning; if there is a flaw in the argument presenting and defending corrected reasoning Response may include: a logical approach based on a conjecture and/or stated assumptions, utilizing mathematical connections (when appropriate) an efficient and logical progression of steps with appropriate justification precision of calculation correct use of grade-level vocabulary, symbols and labels justification of a conclusion evaluation of whether an argument or conclusion is generalizable evaluating, interpreting and critiquing the validity of other's responses, approaches and reasoning, and providing a counter-example where applicable. 	 reasoning, using symbols such as equal signs appropriately distinguishing correct explanation/reasoning from that which is flawed identifying and describing the flaw in reasoning or describing errors in solutions to multi-step problems presenting corrected reasoning Response may include: a logical approach based on a conjecture and/or stated assumptions, utilizing mathematical connections (when appropriate) a logical progression of steps precision of calculation correct use of grade-level vocabulary, symbols and labels justification of whether an argument or conclusion is generalizable evaluating, interpreting and critiquing the validity of other's responses, approaches and reasoning. 	 symbols such as equal signs appropriately distinguishing correct explanation/reasoning from that which is flawed identifying and describing the flaw in reasoning or describing errors in solutions to multi-step problems presenting corrected reasoning Response may include: a logical approach based on a conjecture and/or stated assumptions a logical, but incomplete, progression of steps minor calculation errors some use of grade-level vocabulary, symbols and labels partial justification of a conclusion based on own calculations evaluating the validity of other's responses, approaches and conclusions. 	reasoning, sometimes using symbols such as equal signs appropriately • distinguishing correct explanation/reasoning from that which is flawed • identifying an error in reasoning Response may include: • a conjecture based on faulty assumptions • an incomplete or illogical progression of steps • an intrusive calculation error • limited use of grade-level vocabulary, symbols and labels • partial justification of a conclusion based on own calculations • accepting the validity of other's responses.

	Grade 4 Math: Sub-Claim D In connection with content, the student solves real-world problems with a degree of difficulty appropriate to the grade/course by applying knowledge and skills articulated in the standards for the current grade/course (or for more complex problems, knowledge and skills articulated in the standards for previous grades/courses), engaging particularly in the Modeling practice, and where helpful making sense of problems and persevering to solve them, reasoning abstractly and quantitatively, using appropriate tools strategically, looking for the making use of structure and/or looking for and expressing regularity in repeated reasoning.				
	Level 5: Exceeded Expectations	Level 4: Met Expectations	••••••	Level 2: Partially Met Expectations	
Modeling 4.D.1 4.D.2	 In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by: using stated assumptions or making assumptions and using approximations to simplify a real- world situation analyzing and/or creating constraints, relationships and goals mapping relationships between important quantities by selecting appropriate tools to create models analyzing relationships mathematically between important quantities to draw conclusions justifying and defending models 	 In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by: using stated assumptions or making assumptions and using approximations to simplify a real- world situation mapping relationships between important quantities by selecting appropriate tools to create models analyzing relationships mathematically between important quantities to draw conclusions interpreting mathematical results in the context of the situation reflecting on whether the results make sense 	In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by: • using stated assumptions and approximations to simplify a real- world situation • illustrating relationships between important quantities by using provided tools to create models • analyzing relationships mathematically between important quantities to draw conclusions • interpreting mathematical results in a simplified context reflecting on whether the results make sense • modifying the model if it has not	 In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by: using stated assumptions and approximations to simplify a real- world situation identifying important quantities using provided tools to create models analyzing relationships mathematically to draw conclusions writing an arithmetic expression or equation to describe a situation 	
	 which lead to a conclusion interpreting mathematical results in the context of the situation reflecting on whether the results make sense improving the model if it has not 	 modifying and/or improving the model if it has not served its purpose writing an arithmetic expression or equation to describe a situation 	 served its purpose writing an arithmetic expression or equation to describe a situation 		

Grade 4 Math: Sub-Claim D In connection with content, the student solves real-world problems with a degree of difficulty appropriate to the grade/course by applying knowledge and skills articulated in the standards for the current grade/course (or for more complex problems, knowledge and skills articulated in the standards for previous grades/courses), engaging particularly in the Modeling practice, and where helpful making sense of problems and persevering to solve them, reasoning abstractly and quantitatively, using appropriate tools strategically, looking for the making use of structure and/or looking for and expressing regularity in repeated reasoning.					
Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations		
served its purpose					
 writing a concise arithmetic 					
expression or equation to					
describe a situation					