## CMAS Grade 3 Mathematics Performance Level Descriptors (Based on PARCC)

In 2018, Colorado will continue to use the performance level descriptors (PLDs) that were developed in collaboration with the Partnership for Assessment of Readiness for College and Careers (PARCC) consortium to describe performance on the CMAS assessments.

	Grade 3 Math : Sub-Claim A The student solves problems involving the Major Content for the grade/course with connections to the Standards for Mathematical Practice.			
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Quotients	Understands and interprets products and quotients of whole numbers.		Interprets products and quotients of whole numbers.	Determines products and quotients of whole numbers within 100.
3.0A .2 3.0A .4 3.0A .6 3.0A.7-1 3.0A.7-2	Determines the unknown whole number in a multiplication or division problem by relating	number in a multiplication or division problem by relating multiplication and division. <b>One</b> factor is greater than or equal to 5.	number in a multiplication or division problem by relating multiplication and division, with both factors less than or equal to 5,	Determines the unknown whole number in a multiplication or division problem by relating multiplication and division, with both factors less than or equal to 5, or with one factor of 10.
		within 100, using strategies relating multiplication and division or	Multiplies and divides within 100, using strategies relating multiplication and division or properties of operations.	
Multiplication and Division 3.0A.3-1	Uses multiplication and division within 100 to solve word problems involving equal groups, arrays, area, and measurement quantities	within 100 to solve word problems involving equal groups and arrays. One factor is greater than or equal to 5.	100 to solve word problems involving equal groups <b>and arrays</b> , with both factors less than or equal	Given a visual aid, uses multiplication and division within 100 to solve word problems involving equal groups. Both factors are less than or equal to 5, with both factors less than or equal to 5, or with one factor of 10.
	Identifies multiple contexts given			

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	a numerical expression involving multiplication and division.				
Two-Step Problems 3.OA.8 3.Int.1 3.Int.2	Solves two-step <b>unscaffolded</b> word problems using the four operations, <b>including rounding</b> <b>where appropriate</b> , in which the unknown is in a variety of positions. <b>Both values</b> for each operation performed is substantial (towards the upper limits as	problems using the four operations in which the unknown is in a variety of positions. One of the values for each operation performed is substantial (towards	problems using the four operations and in which the sum, difference, product or quotient is always the unknown. One of the values for each operation performed is substantial (towards the upper limits as defined by the standard	Solves two-step scaffolded word problems using the four operations and in which the sum, difference, product or quotient is always the unknown.	
Fraction Equivalence 3.NF.3a-1 3.NF.3a-2 3.NF.3b-1 3.NF-3c 3.NF-3d 3.NF-3d 3.NF.A.Int.1	generates equivalent fractions with denominators of 2, 3, 4, 6 and 8.		equivalent fractions with denominators of 2, 4 and 8.	Given a visual model recognizes equivalent fractions with denominators of 2, 4 and 8. Expresses the number 1 as a fraction.	
	Compares two fractions that have the same numerator or same denominator using symbols to justify conclusions. <b>Plots the</b>	Compares two fractions that have the same numerator or same denominator using symbols <b>and</b> <b>justifies conclusions by using a</b> <b>visual model.</b> The student must recognize that two fractions must refer to the same whole in order to compare.	Compares two fractions that have the same numerator or same denominator using symbols. The student must recognize that two fractions must refer to the same whole in order to compare.		
	Given a whole number and two fractions in a real-world situation, plots all three numbers on a				

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	number line and determines which fraction is closest to the whole number. Justifies the comparison by plotting points on a number line.					
Fractions as Numbers 3.NF.1 3.NF.2 3.NF.A.Int.1	equal parts – limiting the	Understands 1/b is equal to one whole that is partitioned into b equal parts – limiting the denominators to 2, 4 and <b>8</b> .	Understands 1/ <i>b</i> is equal to one whole that is partitioned into <i>b</i> equal parts – limiting the denominators to 2 and 4.	Understands 1/b is equal to one whole that is partitioned into b equal parts – limiting the denominators to 2 and 4.		
	diagram by partitioning the number line between 0-1 into <i>b</i> equal parts recognizing that <i>b</i> is the	Represents 1/b on a number line diagram by partitioning the number line between 0-1 into b equal parts recognizing that b is the total number of parts.	Represents 1/b on a number line diagram by partitioning the number line between 0-1 into b equal parts recognizing that b is the total number of parts.	Identifies 1/ <i>b</i> on a number line diagram when partitioned between 0 and 1 into <i>b</i> equal parts.		
	the quantity $a/b$ by marking off $a$		Represents fractions in the form <i>a/b</i> using a visual model.			
	Applies the concepts of 1/b and a/b in real-world situations.					
	Describes the number line that best fits the context.					
<b>Time</b> 3.MD.1-1 3.MD.1-2	Tells, writes and measures time to the nearest minute.	Tells, writes and measures time to the nearest minute.	Tells, writes and measures time to the nearest minute.	Tells, writes and measures time to the nearest minute.		
			Solves one-step word problems involving addition or subtraction			

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	of time intervals in minutes.		of time intervals in minutes, with scaffolding, such as a number line diagram.	
Volumes and Masses 3.MD.2-1 3.MD.2-2 3.MD.2-3 3.Int.5	multi-step word problems involving liquid volumes and masses of objects using any of the four basic operations. Number values should be towards the higher end of the acceptable values for each operation.	Using grams, kilograms or liters, measures and estimates liquid volumes and masses of objects using any of the four basic operations. Uses estimated measurements, when indicated, to answer one- step word problems.	•	Using grams, kilograms or liters, measures liquid volumes and masses of concrete objects (beakers, measuring cups, scales).
Geometric Measurement 3.MD.5 3.MD.6 3.MD.7b-1 3.MD.7d	plane figures. Understands area is measured using square units. <b>Describes a</b> visual model to show understanding that area that can be found by covering a plane figure	plane figures. With a visual model, understands area is measured using square units. Determines area by covering a plane figure without gaps or	plane figures. With a visual model, understands	Recognizes area as an attribute of plane figures. With a visual model, understands area is measured using square units. Determines area by counting unit squares.

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	Represents the area of a plane figure as "n" square units.		

	Grade 3 Math: Sub-Claim B The student solves problems involving the Additional and Supporting Content for the grade/course with connections to the Standards for Mathematical Practice.			
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Arithmetic 3.NBT.2 3.NBT.3	within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction. Multiplies one-digit whole numbers by multiples of 10 in the range 10- 90 using strategies based on place value	algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction. Uses repeated addition to multiply one-digit whole numbers by multiples of 10 in the range 10-90 <b>using strategies based on place</b>	based on place value, properties of operations with scaffolding, and/or	Adds and subtracts within 1000, using strategies and algorithms based on place value, properties of operations with scaffolding, and/or the relationship between addition and subtraction.
Scaled Graphs	Completes a scaled picture graph	Completes a scaled picture graph	Completes a scaled picture graph	Identifies a correctly scaled picture
3.MD.3-1	and a scaled bar graph to represent	and a scaled bar graph to	and a scaled bar graph to	graph and a correctly scaled bar
3.MD.3-3 3.Int.4	a data set.	represent a data set.	represent a data set, with scaffolding, such as using a model	graph to represent a data set.
	many more" and "how many less" problems, <b>requiring a substantial</b> addition, subtraction or multiplication step, using information presented in scaled bar graphs.	many more" and "how many less" problems using information presented in scaled bar graphs.	Solves one-step "how many more" and "how many less" problems using information presented in scaled bar graphs.	Solves one-step "how many more" and "how many less" problems using information presented in scaled bar graphs.
	-	-	Generates measurement data by measuring lengths to the nearest	Identifies correct measurement from figures with appropriate scale

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3.MD.4	half and <b>fourth</b> inch.	half inch.	half inch.	provided.	
	Shows the data by making a line	Shows the data by making a line	Shows the data by making a line		
	plot, where the horizontal scale is	plot, where the horizontal scale is	plot, where the horizontal scale is		
	marked in appropriate units of	marked in appropriate units of	marked in appropriate units of		
	whole numbers, halves <b>or quarters</b> .	whole numbers or halves.	whole numbers or halves, with scaffolding.		
	Uses the line plot to answer				
	questions or solve problems.				
Understandin	Understands the properties of	Understands the properties of	Identifies examples of	Identifies examples of	
g Shapes	quadrilaterals and the	quadrilaterals and the	quadrilaterals and the	quadrilaterals and the	
3.G.1	subcategories of quadrilaterals.	subcategories of quadrilaterals.	subcategories of quadrilaterals.	subcategories of quadrilaterals.	
	Recognizes and sorts examples of	Recognizes examples of	Recognizes examples of		
	quadrilaterals that have shared	quadrilaterals that have shared	quadrilaterals that have shared		
	attributes and <b>shows</b> that the	attributes and that the shared	attributes and that the shared		
	shared attributes can define a	attributes can define a larger	attributes can define a larger		
	larger category.	category.	category.		
	Draws examples and <b>non-examples</b>				
	attributes.	with specific attributes.			
Perimeter and		Solves mathematical problems	Solves mathematical problems	Solves mathematical problems	
Area		involving perimeters of polygons,	involving perimeters of polygons,	involving perimeters of polygons,	
3.G.2		including finding the perimeter	including finding the perimeter	including finding the perimeter	
3.MD.8		given the side lengths, finding an	given the side lengths, and	given the side lengths.	
3.Int.3		unknown side length, and provides			
		examples of rectangles with the	same area and different		
	8	same area and different	perimeters.		
	perimeter and different areas or	perimeters.			
	with the same area and different				
	perimeters.				

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A substantial addition, subtraction, or multiplication step with number values towards the higher end of the acceptable values for each operation			
Partitions shapes into parts with equal areas and expresses the area as a unit fraction of the whole.			

		udent expresses grade/course-level	h: Sub-Claim C appropriate mathematical reasoning to precision when making mathema	
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
Properties of Operations 3.C.1-1 3.C.1-2 3.C.1-3 3.C.2	<ul> <li>knowledge, skills, and abilities</li> <li>described in Sub-claims A and B,</li> <li>the student clearly constructs and</li> <li>communicates a complete written</li> <li>response based on</li> <li>explanations/reasoning using the:</li> <li>properties of operations</li> <li>relationship between addition</li> <li>and subtraction</li> <li>relationship between</li> <li>multiplication and division</li> <li>identification of arithmetic</li> <li>patterns</li> <li>Response may include:</li> </ul>	<ul> <li>In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student clearly constructs and communicates a complete written response based on explanations/reasoning using the:</li> <li>properties of operations</li> <li>relationship between addition and subtraction</li> <li>relationship between multiplication and division</li> <li>identification of arithmetic patterns</li> <li>Response may include:</li> <li>a logical/defensible approach based on a conjecture and/or stated assumptions, utilizing</li> </ul>	<ul> <li>In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student constructs and communicates a written response based on explanations/reasoning using the:</li> <li>properties of operations</li> <li>relationship between addition and subtraction</li> <li>relationship between multiplication and division</li> <li>identification of arithmetic patterns</li> <li>Response may include:</li> <li>a logical approach based on a conjecture and/or stated assumptions</li> </ul>	In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student constructs and communicates an incomplete written response based on explanations/reasoning using the: • properties of operations • relationship between addition and subtraction • relationship between multiplication and division • identification of arithmetic patterns Response may include: • an approach based on a conjecture and/or stated or faulty assumptions • an incomplete or illogical

			n: Sub-Claim C	
			appropriate mathematical reasoning to precision when making mathematical section when mathematical section whe	
	Level 5: Exceeded Expectations	Level 4: Met Expectations		Level 2: Partially Met Expectations
	<ul> <li>appropriate)</li> <li>an efficient and logical progression of steps with appropriate justification</li> <li>precision of calculation</li> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> </ul>	<ul> <li>mathematical connections (when appropriate)</li> <li>a logical progression of steps</li> <li>precision of calculation</li> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> </ul>	<ul> <li>a logical, but incomplete, progression of steps</li> <li>minor calculation errors</li> <li>limited use of grade-level vocabulary, symbols and labels</li> <li>partial justification of a conclusion based on own calculations</li> </ul>	progression of steps • an intrusive calculation error • limited use of grade-level vocabulary, symbols and labels • partial justification of a conclusion based on own calculations
	<ul> <li>determination of whether an argument or conclusion is generalizable</li> <li>evaluating, interpreting and critiquing the validity of other's responses, reasonings, and approaches, utilizing mathematical connections (when appropriate). Provides a counter-example where applicable.</li> </ul>	<ul> <li>evaluating, interpreting and critiquing the validity of other's responses, reasonings, and approaches, utilizing mathematical connections (when appropriate).</li> </ul>	<ul> <li>evaluating the validity of other's responses, approaches and conclusions.</li> </ul>	
Concrete	In connection with the content	In connection with the content	In connection with the content	In connection with the content
		knowledge, skills, and abilities	<b>U</b>	knowledge, skills, and abilities
3.C.3-1 3.C.3-2	the student clearly constructs and	described in Sub-claims A and B, the student clearly constructs and communicates a well- <b>organized</b>		described in Sub-claims A and B, the student constructs and communicates <b>an</b> incomplete
3.C.6-2	operations using concrete referents	· · ·	on operations using concrete referents such as diagrams – including number lines (provided in	response based on operations using concrete referents such as diagrams – including number lines
	number lines (whether provided in the prompt or constructed by the student) and connecting the diagrams to a written (symbolic)	number lines (whether provided in	the prompt) – connecting the diagrams to a written (symbolic) method, which may include: • a logical approach based on a	<ul> <li>(provided in the prompt) –</li> <li>connecting the diagrams to a</li> <li>written (symbolic) method, which</li> <li>may include:</li> <li>a conjecture and/or stated or</li> </ul>
	<ul> <li>a logical approach based on a</li> </ul>	<ul> <li>a logical approach based on a</li> </ul>	conjecture and/or stated assumptions	faulty assumptions

	Grade 3 Math: Sub-Claim C			
	In connection with content, the stu	udent expresses grade/course-level	appropriate mathematical reasoning	g by constructing viable arguments,
	critiquing the re	asoning of others and/or attending	to precision when making mathema	tical statements.
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations
	<ul> <li>conjecture and/or stated assumptions, utilizing mathematical connections (when appropriate)</li> <li>an efficient and logical progression of steps with appropriate justification</li> <li>precision of calculation</li> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> <li>determination of whether an argument or conclusion is generalizable</li> <li>evaluating, interpreting, and critiquing the validity of other's responses, approaches, and reasoning, and providing a counter-example where applicable</li> </ul>	<ul> <li>(when appropriate)</li> <li>a logical progression of steps</li> <li>precision of calculation</li> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> <li>evaluating, interpreting, and critiquing the validity of other's responses, approaches, and reasoning.</li> </ul>	<ul> <li>a logical, but incomplete, progression of steps</li> <li>minor calculation errors</li> <li>some use of grade-level vocabulary, symbols and labels</li> <li>partial justification of a conclusion based on own calculations.</li> <li>evaluating the validity of other's responses, approaches and conclusions</li> </ul>	<ul> <li>an incomplete or illogical progression of steps</li> <li>an intrusive calculation error</li> <li>limited use of grade-level vocabulary, symbols and labels</li> <li>partial justification of a conclusion based on own calculations</li> <li>accepting the validity of other's responses</li> </ul>
Distinguish	In connection with the content		In connection with the content	In connection with the content
Correct	-	_	-	knowledge, skills, and abilities
Explanation/				described in Sub-claims A and B,
Reasoning	the student clearly constructs and	the student <b>clearly</b> constructs and	the student constructs and	the student constructs and
from that	communicates a well-organized	communicates a well-organized	communicates a <b>complete</b>	communicates an incomplete
which is	and complete response by:	and complete response by:	response by:	response by:
Flawed	<ul> <li>presenting and defending</li> </ul>	<ul> <li>presenting and defending</li> </ul>	<ul> <li>presenting solutions to multi-</li> </ul>	<ul> <li>presenting solutions to</li> </ul>
3.C.4-1	solutions to multi-step problems	solutions to multi-step problems	<b>step</b> problems in the form of	scaffolded two-step problems in
3.C.4-2	in the form of valid chains of	in the form of valid chains of	valid chains of reasoning, using	the form of valid chains of
3.C.4-3	reasoning, using symbols such as	reasoning, using symbols such as	symbols such as equal signs	reasoning, sometimes using
3.C.4-4	equal signs appropriately	equal signs appropriately	appropriately	symbols such as equal signs
3.C.4-5	• evaluating	<ul> <li>distinguishing correct</li> </ul>	<ul> <li>distinguishing correct</li> </ul>	appropriately
3.C.4-6	explanation/reasoning; if there is	explanation/reasoning from that		

		Grade 3 Math: Sub-Claim C In connection with content, the student expresses grade/course-level appropriate mathematical reasoning by constructing viable arguments,				
	critiquing the reasoning of others and/or attending to precision when making mathematical statements. Level 5: Exceeded Expectations Level 4: Met Expectations Level 3: Approached Expectations Level 2: Partially Met Expectation					
3.C.5-1 3.C.5-2 3.C.4-7	<ul> <li>a flaw in the argument</li> <li>presenting and defending corrected reasoning</li> <li>Response may include:</li> <li>a logical approach based on a conjecture and/or stated</li> </ul>	<ul> <li>which is flawed</li> <li>identifying and describing the flaw in reasoning or describing errors in solutions to multi-step problems</li> <li>presenting corrected reasoning Response may include:</li> </ul>	<ul> <li>which is flawed</li> <li>identifying and describing the flaw in reasoning or describing errors in solutions to multi-step problems</li> <li>presenting corrected reasoning Response may include:</li> <li>a logical approach based on a conjecture and/or stated assumptions</li> <li>a logical, but incomplete, progression of steps</li> <li>minor calculation errors</li> </ul>	explanation/reasoning from that which is flawed • identifying an error in reasoning		
	<ul> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> <li>evaluation of whether an argument or conclusion is generalizable</li> <li>evaluating, interpreting, and critiquing the validity of other's responses, approaches and reasoning, and providing a counter-example where applicable.</li> </ul>	<ul> <li>correct use of grade-level vocabulary, symbols and labels</li> <li>justification of a conclusion</li> <li>evaluating, interpreting and critiquing the validity of other's responses, approaches and reasoning.</li> </ul>	<ul> <li>some use of grade-level vocabulary, symbols and labels</li> <li>partial justification of a conclusion based on own calculations</li> <li>evaluating the validity of other's responses, approaches and conclusions.</li> </ul>	<ul> <li>limited use of grade-level vocabulary, symbols and labels</li> <li>partial justification of a conclusion based on own calculations</li> <li>accepting the validity of other's responses</li> </ul>		

	Grade 3 Math: Sub-Claim D In connection with content, the student solves real-world problems with a degree of difficulty appropriate to the grade/course by applying knowledge and skills articulated in the standards for the current grade/course (or for more complex problems, knowledge and skills articulated in the standards for previous grades/courses), engaging particularly in the Modeling practice, and where helpful making sense of problems and persevering to solve them, reasoning abstractly and quantitatively, using appropriate tools strategically, looking for the making use of structure and/or looking for and expressing regularity in repeated reasoning.				
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations	
Modeling 3.D.1 3.D.2	In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word	<ul> <li>In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by:</li> <li>using stated assumptions or making assumptions and using approximations to simplify a real-world situation</li> <li>mapping relationships between important quantities by selecting appropriate tools to create models</li> <li>analyzing relationships mathematically between important quantities to draw conclusions</li> <li>interpreting mathematical results in the context of the situation</li> </ul>	In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and applies mathematics to solve multi- step, real-world contextual word problems by • using stated assumptions and approximations to simplify a real-world situation • illustrating relationships between important quantities by using provided tools to create models • analyzing relationships mathematically between important quantities to draw conclusions • interpreting mathematical results in a simplified context • reflecting on whether the results make sense • modifying the model if it has not served its purpose	In connection with the content knowledge, skills, and abilities described in Sub-claims A and B, the student devises a plan and	
	<ul> <li>interpreting mathematical results in the context of the</li> </ul>	<ul> <li>modifying and/or improving the model if it has not served its purpose</li> </ul>	• writing an arithmetic expression or equation to describe a		

	Grade 3 Math: Sub-Claim D In connection with content, the student solves real-world problems with a degree of difficulty appropriate to the grade/course by applying knowledge and skills articulated in the standards for the current grade/course (or for more complex problems, knowledge and skills articulated in the standards for previous grades/courses), engaging particularly in the Modeling practice, and where helpful making sense of problems and persevering to solve them, reasoning abstractly and quantitatively, using appropriate tools strategically, looking for the making use of structure, and/or looking for and expressing regularity in repeated reasoning.					
	Level 5: Exceeded Expectations	Level 4: Met Expectations	Level 3: Approached Expectations	Level 2: Partially Met Expectations		
	<ul> <li>writing a concise arithmetic</li> </ul>					
	expression or equation to					
	describe a situation					